



University of Pittsburgh

# **Virtual Inertia: Designing Power Electronic Systems to Behave like Synchronous Machines**

**Power Electronics Workshop  
Sandia National Lab**

**July 18, 2018 – Albuquerque, New Mexico**

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## University of Pittsburgh Energy GRID Institute

*Leadership in this sector is part of Pittsburgh's Heritage; and advancing this legacy is now part of our Responsibility.*

### The Vision:

- 1 – Create a national/international consortium focused on serving the electric utility industry and government entities (ONR, DoD, DoE, etc).
- 2 – Evaluate and assess both major industry-wide and individual issues and grand challenges.
- 3 – Work in collaboration with various partners towards the development, demonstration, and first-generation deployment of solutions across a broad area of grid technologies, systems, designs, operations, and regulation, as well as addressing market forces and business considerations.

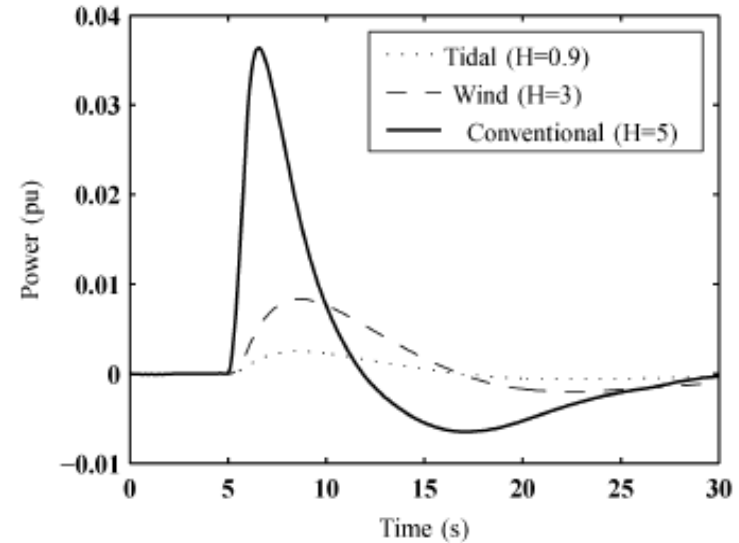
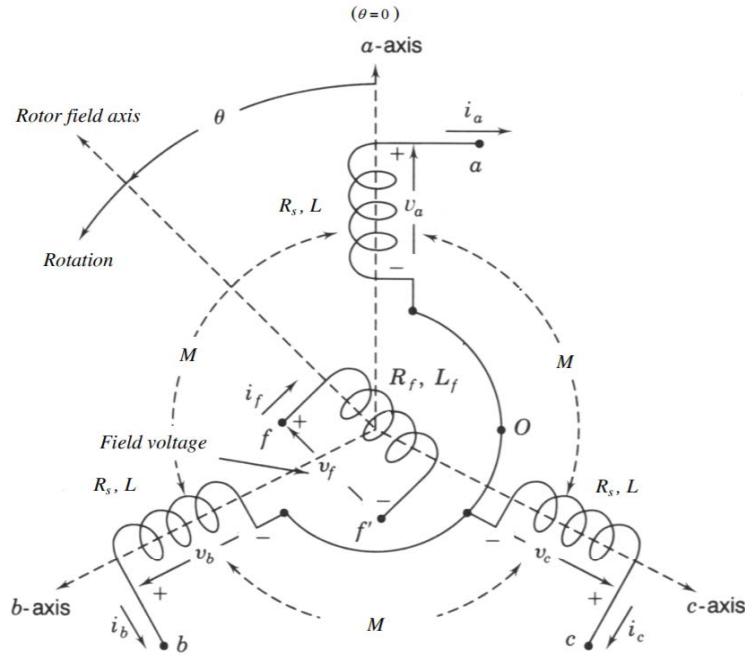


13.8 kV / 4.16kV portion of High Voltage Laboratory at the University of Pittsburgh GRID Institute



# Benefits of System Inertia

# Review of Mechanical Inertia



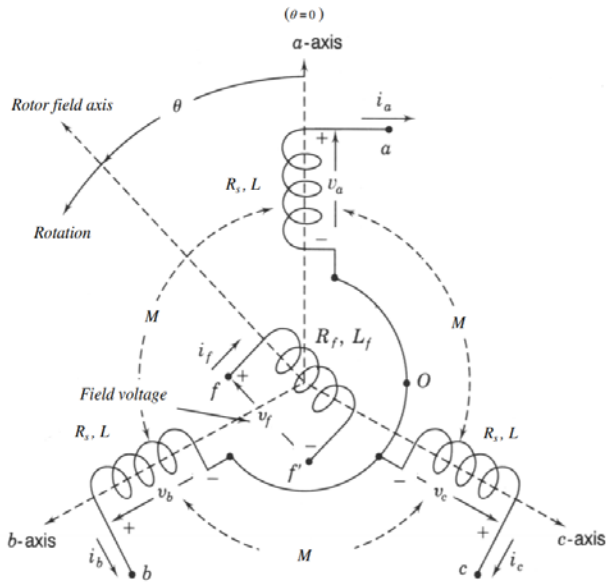
The inertia constant,  $H$ , is the amount of stored kinetic energy in the turbine and generator system and is defined below.

$$H = \frac{J\omega_0^2}{2S_N}$$

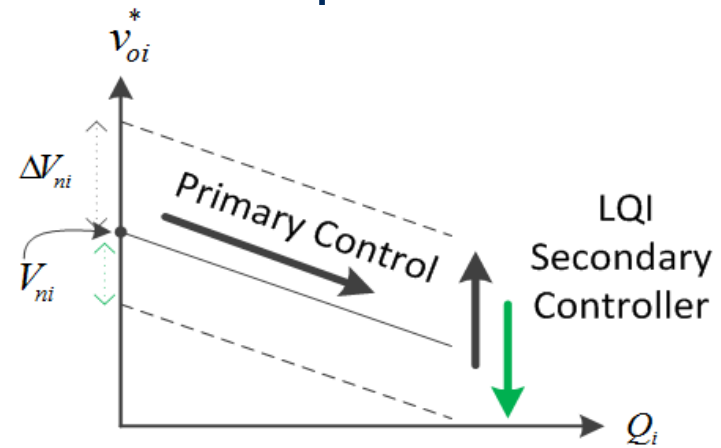
A. Mullane, G. Bryans, and M. O'Malley, "Kinetic energy and frequency response comparison for renewable generation systems," in *2005 International Conference on Future Power Systems*, 2005, p. 6

Q.-C. Zhong and G. Weiss, "Static synchronous generators for distributed generation and renewable energy," in *2009 IEEE/PES Power Systems Conference and Exposition*, 2009, pp. 1-6.

# Synchronizing Electric Machines to the Electric Grid

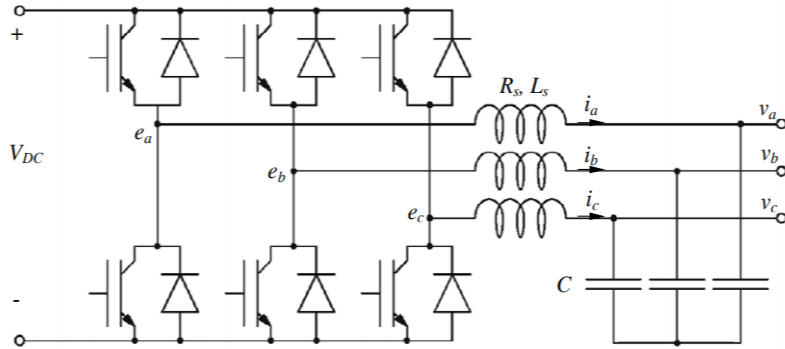


## Droop Curves





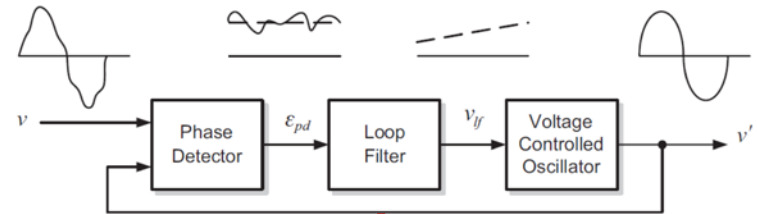
# Synchronizing Power Electronics to the Power Grid



Option #1

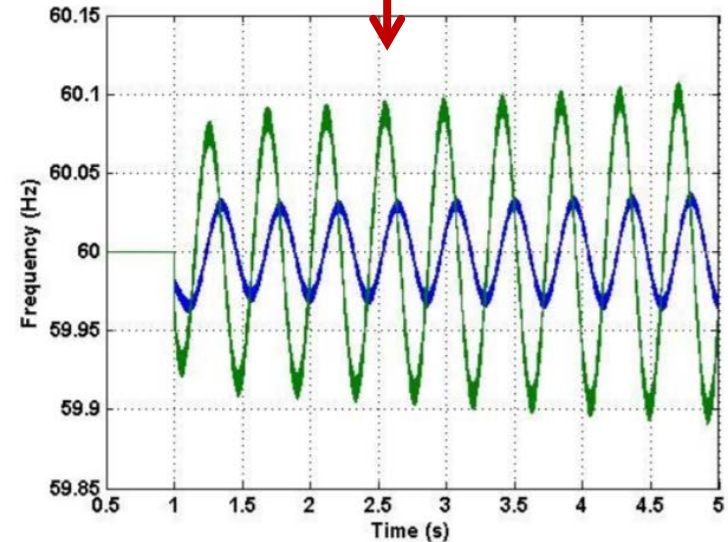
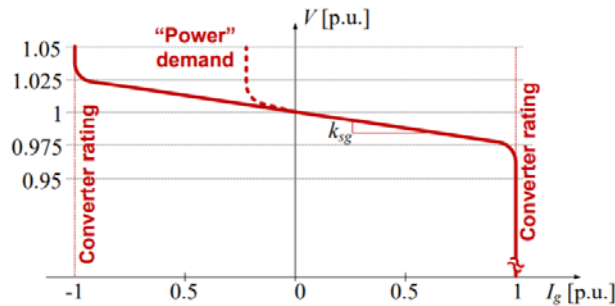


Phase Lock Loops  
(Stability Concerns)



Option #2

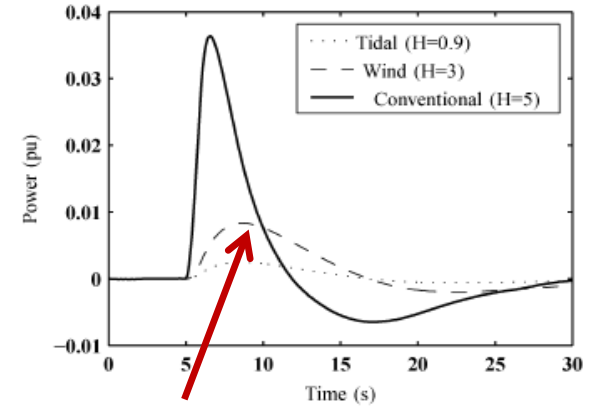
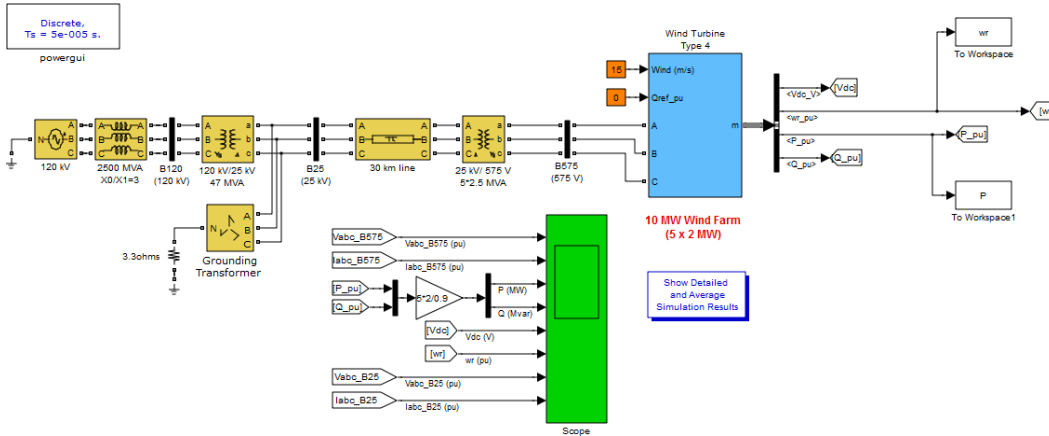
Static Droop



D. Dong, "AC-DC Bus-Interface Bi-directional Converters in Renewable Energy Systems," PhD Dissertation, Virginia Tech, 2012.

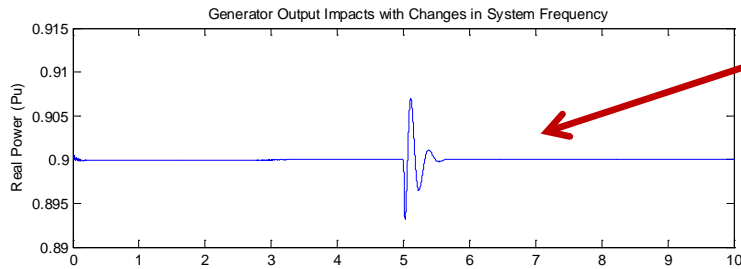
I. Cvetkovic, "Modeling, Analysis, and Design of Renewable Energy Nanogrid Systems," MS Thesis, Virginia Tech, 2010.

# Power Electronic Decoupling & Impacts on System Behavior

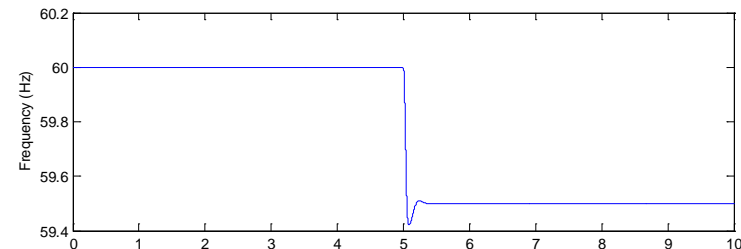


Full Converter Interface

Wind Turbine Set-Up in Simulink Demo Models



Generator not dynamically responding (decoupled) with frequency change.



### Other Areas

1. **HVDC Grids** – decoupling effect is **beneficial** to prevent widespread system impacts.
2. **Microgrids** – **Warning**. Nominal current and fault current are on the same order of magnitude because the inertia response is not prominent.

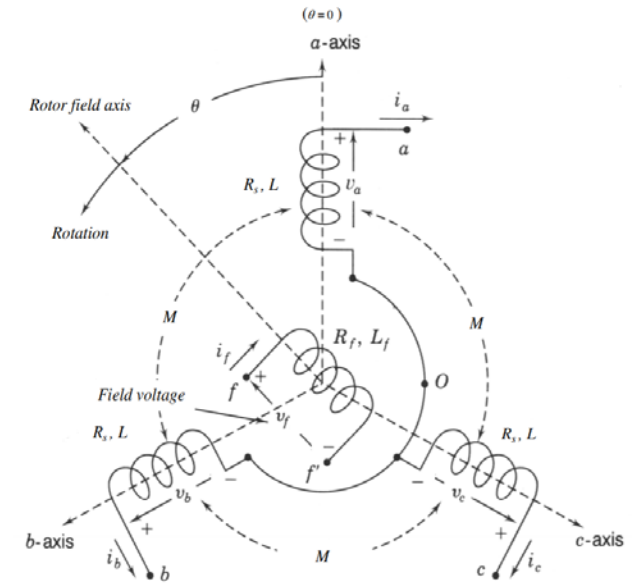
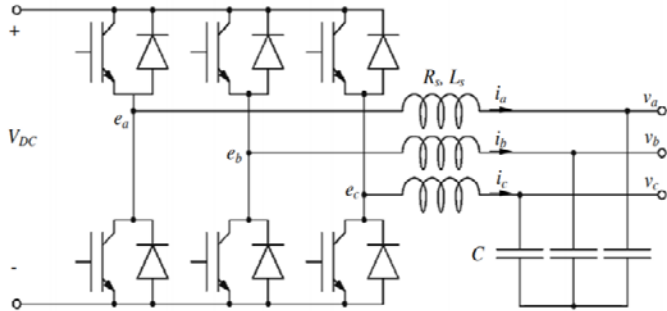


# Growing Trend of Virtual Inertia



# Virtual Synchronous Machine Control

How can we make power electronics behave like synchronous machines? **Through system control.**



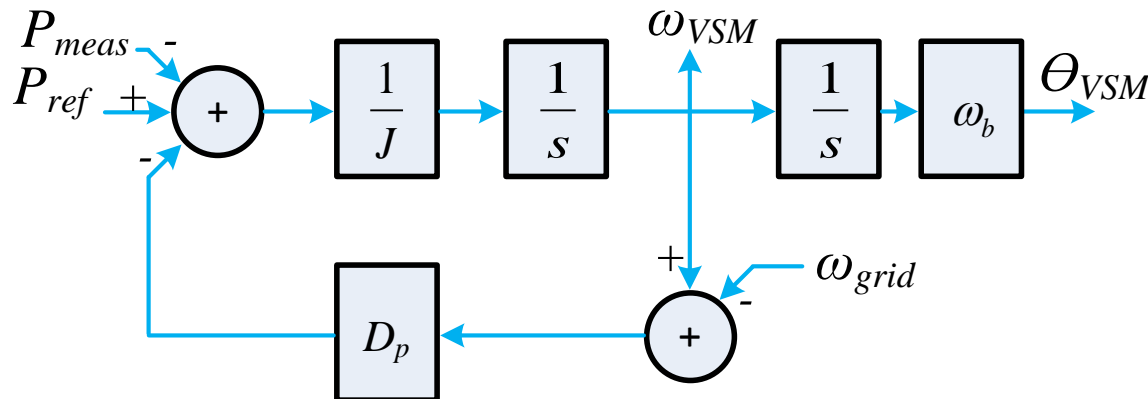
Mechanical systems		Electrical systems
Torque $T$	$\equiv$	Current $I_{dc}$
Angular speed $\Omega$	$\equiv$	Voltage $v_{dc}$
Moment of Inertia $J$	$\equiv$	Capacitance $C$
Friction $k_f$	$\equiv$	Conductance $G$

## Virtual Synchronous Machine Control

- It is well known that a synchronous machine (SM) can synchronize with each other or with the power supply autonomously without the need for external communications.
- VSM control follows the swing equation in order to mimic the desirable inertial dynamics inherent to synchronous machines.

$$J\ddot{\theta} = (T_m - T_e - D_p\dot{\theta})$$

$$\ddot{\theta}_{VSM} = \frac{1}{J} [P_{ref} - P_{meas} - D_p(\omega_{VSM} - \omega_{grid})]$$



Where,  
 $P = T\omega$   
 $\omega = \dot{\theta}$

Swing equation implemented into system control architecture for VSM

# Electrical Stability Performance of the VSM

- Regulation of frequency for a phase disturbance with varying values of damping  $D_p$  and inertia  $J$

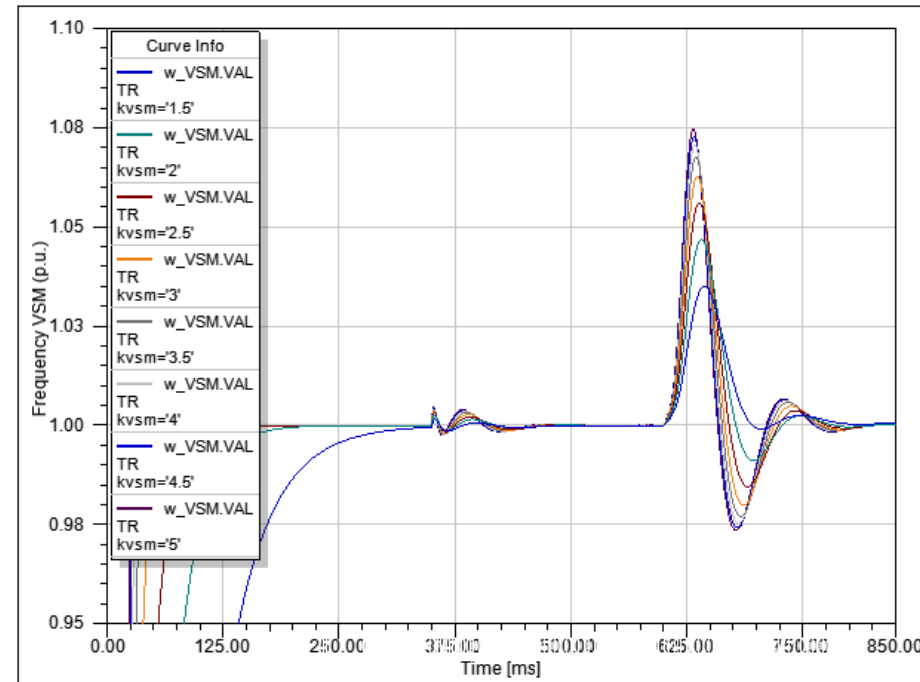
$$Js^2 + D_p s = T_m - T_e = 0$$

$$\rightarrow s(Js + D_p) = 0$$

$$\rightarrow Js = -D_p$$

$$\rightarrow s = -D_p/J$$

Elements	Description	Value
$J$	Moment of inertia	{1.5, 2, 2.5, 3, 3.5, 4, 4.5, 5}
$D_p$	Friction coefficient	{15, 20, 25, 30, 35, 40, 45, 50}
$-D_p/J$	Case ratio with $k_{VSM}$	-10

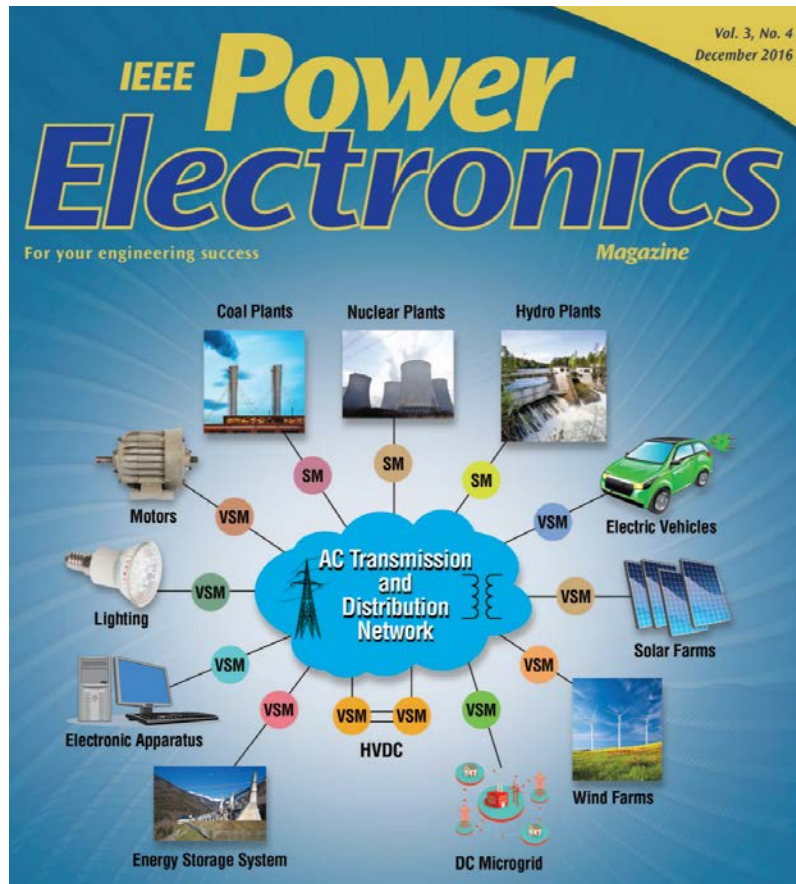


VSM frequency for varying values of  $D_p$  and  $J$



# Concepts Penetrating the Engineering Community

# Academia vs. Practicing Engineers



When first exposed to concept, engineers have asked:

1. Where is the inertia physically coming from for the power electronics system?
2. Are we truly advancing by looking at mimicking a synchronous machine?
3. Is synchroverter a good name given the speed of response of power electronics compared to generators?



**Questions?**





## Contact Information

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